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# Rhombic alternative tableaux, assemblies of permutations, and the ASEP

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## Abstract

In this paper, we introduce the rhombic alternative tableaux, whose weight generating functions provide combinatorial formulae to compute the steady state probabilities of the two-species ASEP. In the ASEP, there are two species of particles, one heavy and one light, on a one-dimensional finite lattice with open boundaries, and the parameters  $a, b$ , and  $q$  describe the hopping probabilities. The rhombic alternative tableaux are enumerated by the Lah numbers, which also enumerate certain assemblies of permutations. We describe a bijection between the rhombic alternative tableaux and these assemblies. We also provide an insertion algorithm that gives a weight generating function for the assemblies. Combined, these results give a bijective proof for the weight generating function for the rhombic alternative tableaux.

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