
Affine type A geometric crystal structure on the Grassmannian

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Abstract

We construct a type $A(1)_{n-1}$ affine geometric crystal structure on the Grassmannian $\text{Gr}(k, n)$. The tropicalization of this structure recovers the combinatorics of crystal operators on semistandard Young tableaux of rectangular shape (with $n - k$ rows), including the affine crystal operator e_0 . In particular, the promotion operation on these tableaux essentially corresponds to cyclically shifting the Plücker coordinates of the Grassmannian.

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