# On intervals of the consecutive pattern poset

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**Résumé**

The consecutive pattern poset is the infinite partially ordered set of all permutations where $\sigma \leq$
$tau$ if
$tau$ has a subsequence of adjacent entries in the same relative order as the entries of $\sigma$. We study the structure of the intervals in this poset from topological, poset-theoretic, and enumerative perspectives. In particular, we prove that all intervals are rank-unimodal and strongly Sperner, and we characterize disconnected and shellable intervals. We also show that most intervals are not shellable and have Mo bius function equal to zero.

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