A bijective proof of Macdonald's reduced word formula

Sara Billey^{*1}, Alexander Holroyd^{*2}, and Benjamin Young^{*3}

¹Department of Mathematics [Seattle] – University of Washington Department of Mathematics Box 354350 Seattle, WA 98195-4350, États-Unis

²Microsoft Research [Redmond] – One Microsoft Way, Redmond, WA 98052, USA, États-Unis ³Department of Mathematics, University of Oregon [Eugene] – Eugene OR 97403 USA, États-Unis

Résumé

We describe a bijective proof of Macdonald's reduced word identity using pipe dreams and Little's bumping algorithm. The proof extends to a principal specialization of the identity due to Fomin and Stanley. Our bijective tools also allow us to address a problem posed by Fomin and Kirillov from 1997, using work of Wachs, Lenart and Serrano- Stump.

*Intervenant